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## Data 88S

Feb 28, 2024

## Chapter 5, Exercise 2

1. A true/false test consists of 25 questions. A student knows the correct answer to 10 of the questions. She guesses each of the other answers independently based on the toss of a coin.
(a) Find the expectation of the number of correct answers.
(b) Find the chance that the student gets more than 20 questions right.

## Chapter 5, Exercise 1

2. Let $X$ have the distribution displayed in the table below.

| $x$ | -2 | -1 | 0 | 1 |
| ---: | :---: | :---: | :---: | :---: |
| $P(X=x)$ | 0.2 | 0.25 | 0.35 | 0.2 |

(a) Find $E(X)$
(b) Find $E(X-1)$
(c) Find $E(|X-1|)$
(d) Find $E\left(|X-1|^{2}\right)$
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## Chapter 5, Exercise 3

3. A box contains four blank index cards and one that has a gold star on it. Cards are drawn one by one at random without replacement until the gold star appears. Let $D$ be the number of cards drawn.
(a) Find the distribution of $D$.
(b) Find $E(D)$.

## Chapter 5, Exercise 5

4. A coin is tossed four times. Let $X$ be the number of heads in the first three tosses and let $Y$ be the number of heads in the last three tosses.
(a) Do $X$ and $Y$ have different distributions? Explain.
(b) Are $X$ and $Y$ independent? Explain.
(c) Make a joint distribution table for $X$ and $Y$. It might help to write out all the possible outcomes of four tosses of a coin, though it is not necessary.
(d) Use your table in Part c to find $P(X=Y)$.
(e) Use your table in Part c to find the marginal distribution of $X$, and check that it is consistent with your answer in Part a.
